

**Mechanical Engineering 635: Advanced Mechanics of Materials**  
Homework 1

1. The stress tensor at a point  $P(x, y, z)$  in a solid is

$$\begin{pmatrix} 120 & 40 & 30 \\ 40 & 150 & 20 \\ 30 & 20 & 100 \end{pmatrix}$$

- (a) Determine the stresses with respect to a set of axes  $x', y', z'$  obtained by a clockwise rotation of  $30^\circ$  about the  $y$  axis.
- (b) Compute the stress invariants for both coordinate systems and verify that they are equal.
- (c) Compute the principal stresses using the unprimed axes  $(x, y, z)$ .
- (d) Find the orientation of the principal planes with respect to the unprimed axes  $(x, y, z)$ .