## Module/Week 6 Homework: Probabilities and Statistics MGMT 5260: Decision-Making Techniques for Managers

Please create a single Excel file with each problem on a separate worksheet tab.

## Problem 1

A fair coin was tossed 3 times. Calculate the probabilities of the following 5 events.
a. Three heads were observed
b. Two heads were observes
c. One head were observed
d. At least two heads were observed
e. No more than two tails were observed

## Problem 2

$11 \%$ of a city's population are illegal emigrants. Two random people were selected. What is the probability that:
a. Both are legal emigrants.
b. Only one is a legal emigrant.
c. Both are illegal emigrants.

## Problem 3

The following table shows frequency of iPads sold per day at a local electronic store in January of the current year. During that month, there was never a day in which more than 5 iPads were sold.

| Number sold per day | Number of Days |
| :---: | :---: |
| 0 | 3 |
| 1 | 5 |
| 2 | 10 |
| 3 | 4 |
| 4 | 6 |
| 5 | 3 |

a. Determine the mean number of iPads sold per day in January.
b. What is the probability that exactly 4 iPads will be sold in a randomly selected day?
c. What is the probability that 1 or 3 iPads will be sold in a randomly selected day?
d. What is the probability that no more than 2 iPads will be sold in a randomly selected day?
e. What is the probability that at least 3 iPads will be sold in a randomly selected day?

## Problem 4

A variable Z is normally distributed with $\mu=54$ and $\sigma=12.3$. Find the following probabilities:
a. $\mathrm{P}(40<\mathrm{Z} \leq 55.7)$
b. $\mathrm{P}(\mathrm{Z}=64.9)$
c. $\mathrm{P}(\mathrm{Z}>54)$
d. $\mathrm{P}(\mathrm{Z}<48.1)$
e. $\mathrm{P}(\mathrm{Z} \neq 63.4)$
f. $\quad P(Z \leq 70)$
g. $\mathrm{P}(\mathrm{Z}<38.2$ OR $\mathrm{Z}>57.3)$

## Problem 5

Using Excel's standard functions:
a. Calculate the mean, variance and standard deviation of the students' grades presented below.
b. Use the descriptive statistics tool and calculate various statistical measures.

| 90 | 93 | 63 | 55 | 93 | 85 | 79 | 95 | 83 | 61 | 82 | 95 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 66 | 51 | 99 | 50 | 95 | 63 | 69 | 90 | 59 | 57 | 63 | 77 |
| 75 | 54 | 69 | 67 | 79 | 52 |  |  |  |  |  |  |

## Problem 6

The life of an electronic transistor is normally distributed with a mean of 500 hours and a standard deviation of 80 hours. Determine the probability that
a. A transistor will last for more than 400 hours?
b. A transistor will last for less than 350 hours?
c. A transistor will last exactly 501 hours?

## Problem 7

The weight of bags of fertilizer is normally distributed with a mean of 50 pounds and standard deviation of 6 pounds. What is the probability that a bag of fertilizer will weigh:
a. Between 45 and 55 pounds?
b. At least 56 pounds?
c. At most 49 pound?

## Problem 8

The amount of time devoted to studying each week by students who achieve grade A in the course is normally distributed with mean of 7.5 hours and standard deviation of 2.1 hours. Find the probability that an A student study time per week is
a. between 7 and 9 hours?
b. less than 5 hours?
c. exactly 6 hours

